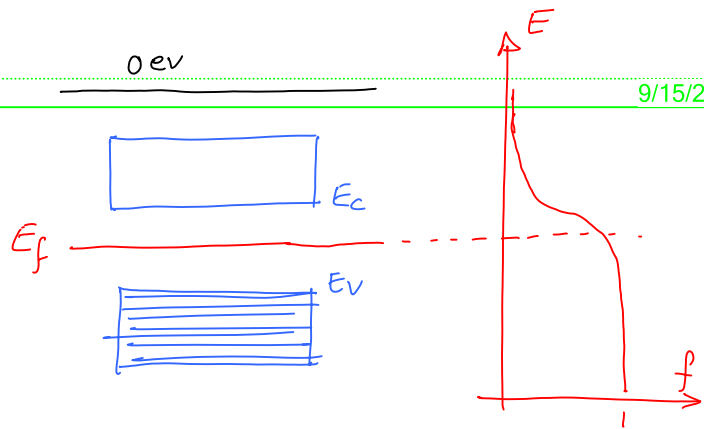
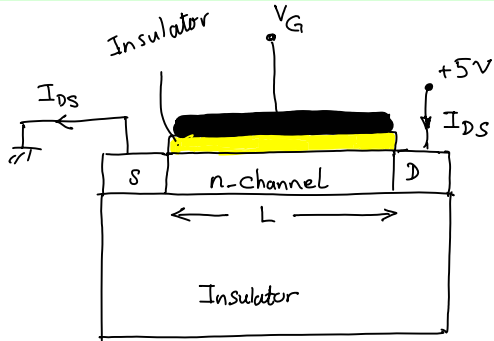


# Session 3

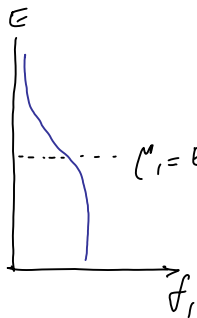
Note Title

9/15/2008



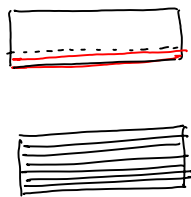
Current depends on number of states around Fermi energy, not on number of electrons.

Source

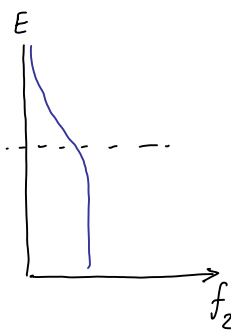


Gate

$V_G < 0$

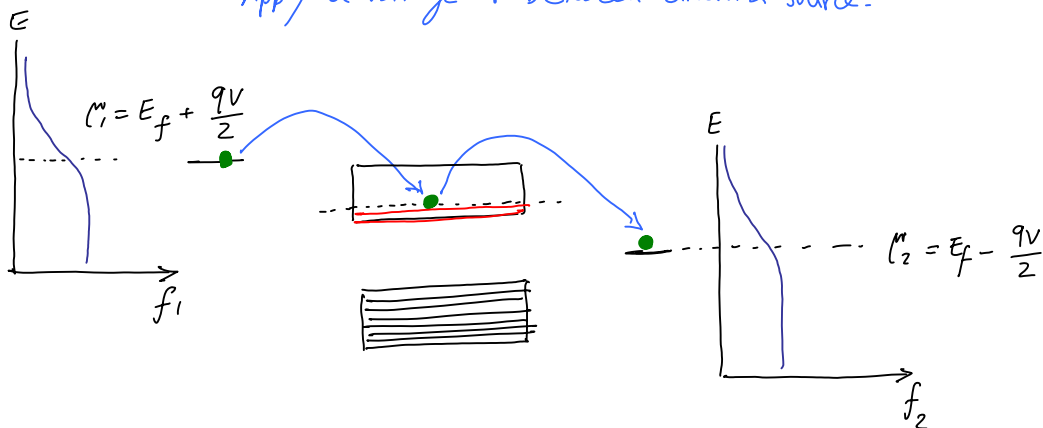


Drain



No current since  $\mu_1 = \mu_2$

Apply a voltage  $V$  between drain & source:

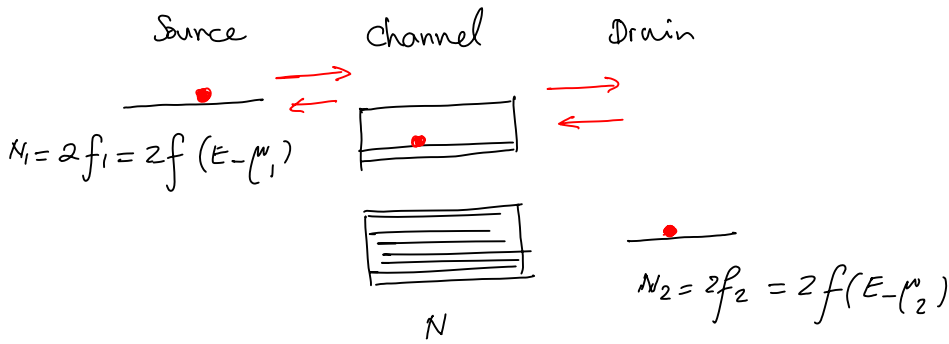


Current flows between source & drain through the energy level

between them. Left side at  $\mu_1$  keeps filling the channel's states and the right side at  $\mu_2$  keeps emptying the channel's states.

If there was no state between  $\mu_1$  &  $\mu_2$  in the channel, there would be no current.

Let's calculate the current for a one level model for source & Drain:



Current from left side:

$$I_1 = e (\text{transition rate from } \mu_1 \text{ to the channel} - \text{transition rate from channel to } \mu_1)$$

$$= e \left( \frac{\gamma_1}{\hbar} N_1 - \frac{\gamma_1}{\hbar} N \right) = e \frac{\gamma_1}{\hbar} (N_1 - N)$$

$\downarrow$                        $\downarrow$                        $\swarrow$   
 rate  $\times$  number                      number of  
 of electrons                      electrons  
 in the source                      in the channel

$$\frac{\gamma}{\hbar} = \frac{\hbar}{2\pi} = \frac{6.626 \times 10^{-34}}{2\pi} = 1.06 \times 10^{-34} \text{ j.s}$$

$$I_2 = e \frac{\gamma_2}{\hbar} (N - N_2)$$

$$\frac{\gamma_i}{\hbar} \left[ \frac{\gamma_i}{j.s} \right] \left[ \frac{1}{s} \right] \rightarrow \gamma_i [j]$$

Say  $\gamma_i = 1 \text{ meV} \rightarrow \frac{\gamma_i}{\hbar} = \frac{10^3 \times 1.6 \times 10^{-19}}{1.06 \times 10^{-34}} \approx 10^{12} \text{ s}^{-1} \rightarrow$  it takes  $\approx 1 \text{ ps}$  for the electron to escape into channel.

Equating  $I_1 = I_2 \Rightarrow$

$$e \frac{\gamma_1}{\hbar} (N_1 - N) = e \frac{\gamma_2}{\hbar} (N - N_2)$$

$$(\gamma_1 + \gamma_2) N = \gamma_1 N_1 + \gamma_2 N_2 \rightarrow N = \frac{\gamma_1 N_1 + \gamma_2 N_2}{\gamma_1 + \gamma_2}$$

$$\Rightarrow I = I_1 = I_2 = \frac{e\gamma_1}{\hbar} \left( N_1 - \frac{\gamma_1 N_1 + \gamma_2 N_2}{\gamma_1 + \gamma_2} \right) = \frac{e\gamma_1}{\hbar} \frac{\gamma_2 (N_1 - N_2)}{\gamma_1 + \gamma_2}$$

$$= \frac{e}{\hbar} \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2} (2f_1(\epsilon) - 2f_2(\epsilon))$$

$$I = \frac{2e}{\hbar} \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2} (f_1(\epsilon) - f_2(\epsilon))$$

So if  $f_1(\varepsilon) = f_2(\varepsilon) \Rightarrow I = 0$  as expected.

$$\begin{array}{ccc} \downarrow & & \downarrow \\ f(\varepsilon - \mu_1) & & f(\varepsilon - \mu_2) \end{array}$$

Let's Taylor expand to get the expression at small voltage:

$$\begin{aligned} f_1(\varepsilon) - f_2(\varepsilon) &= f(\varepsilon - \mu_1) - f(\varepsilon - \mu_2) \\ &= \left[ f(\varepsilon) - \frac{df}{d\varepsilon}(\mu_1) \right] - \left[ f(\varepsilon) - \frac{df}{d\varepsilon}(\mu_2) \right] \\ &= \frac{df}{d\varepsilon} \underbrace{(\mu_2 - \mu_1)}_{-qV_D} = - \frac{df}{d\varepsilon} eV_D \end{aligned}$$

So for small voltage  $V_D$ :

$$I = \frac{2e}{h} \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2} \overbrace{\left( - \frac{df}{d\varepsilon} eV_D \right)}^{f_1 - f_2}$$

$$I = V \underbrace{\frac{2e^2}{h}}_{\substack{\text{dimension of} \\ \text{conductance} \\ [S] \\ \downarrow \\ 1/\Omega}} \underbrace{\frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2}}_{\substack{\text{dimension of} \\ \text{energy} \\ [J]}} \underbrace{\left( - \frac{df}{d\varepsilon} \right)}_{\substack{\text{dimension of} \\ \text{inverse energy} \\ [1/J]}}$$

How does it look?